



FLUENCY AND LANGUAGE

WHAT IS FLUENCY?

*efficient, accurate recall of
a number facts and
procedures is essential FOR
fluency, freeing pupils'
heads to think deeply about
concepts and problems, but
fluency demands more than*





WHAT IS FLUENCY?

requires pupils to have flexibility to move between different contexts and representations of mathematics, to recognise relationships and make connections, and to choose appropriate methods and strategies to solve problems.”

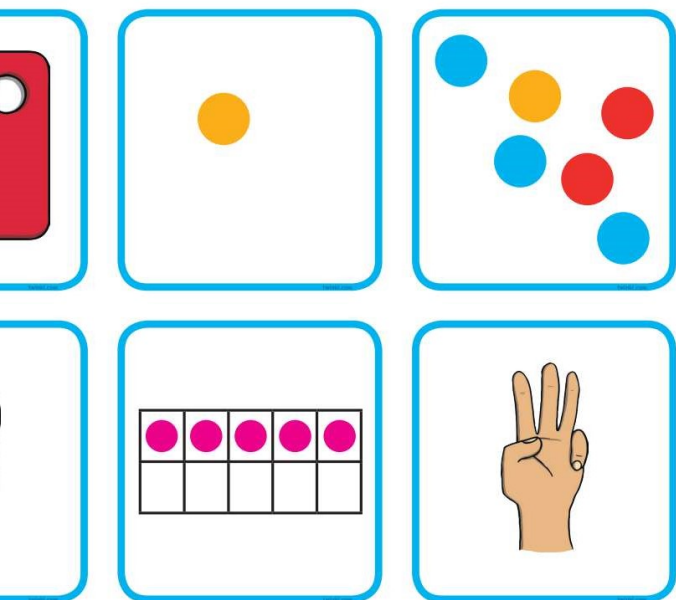
To move between different contexts and representations

To recognise relationships and make connections

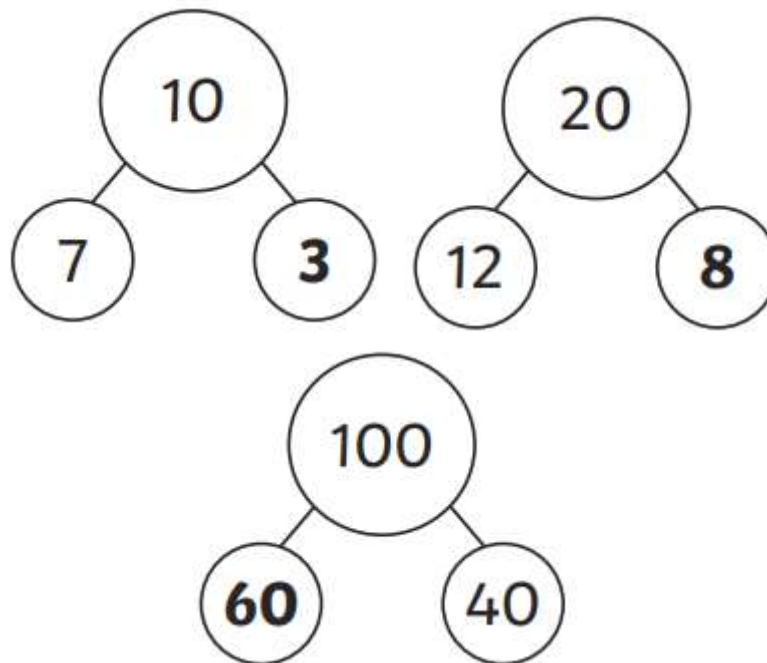
To choose appropriate methods and strategies to solve problems.

WHAT IS MEANT BY KEY NUM FACTS AND PROCEDURES

Subitising



Number bonds



Multiplication table

x	1	2	3	4	5	6	7	8	9
1	1	2	3	4	5	6	7	8	9
2	2	4	6	8	10	12	14	16	18
3	3	6	9	12	15	18	21	24	27
4	4	8	12	16	20	24	28	32	36
5	5	10	15	20	25	30	35	40	45
6	6	12	18	24	30	36	42	48	54
7	7	14	21	28	35	42	49	56	63
8	8	16	24	32	40	48	56	64	72
9	9	18	27	36	45	54	63	72	81
10	10	20	30	40	50	60	70	80	90
11	11	22	33	44	55	66	77	88	99
12	12	24	36	48	60	72	84	96	108



THE OUTCOMES WHEN FLUENCY IS NOT DEVELOPED

Younger pupils' inability to subitise or easily recall addition facts hampers their progress. They may be able to understand a teacher's instruction in, for example, Year 2 or 3, but they struggle to complete tasks with the speed and accuracy of their peers. They eventually obtain the correct answers ('getting by'), thus demonstrating their understanding, but are less likely to remember this new knowledge. This cycle continues, but with pupils increasingly unable to understand, let alone apply, new knowledge. This is likely to be one of the reasons why interventions are so ubiquitous in Year 6: pupils' internal struggles manifest after a significant amount of time has elapsed.



LET'S THINK...

John knows 7×12 is 84.

Mary works out 7×12 by doing 7×10 and 7×2 , then adding the products together."

Who is the better mathematician? Why?



EARNING FACTS IS A JOURNEY.

Start by having a strategy to work it out and understanding the mathematical structures behind it.

Practice until you reach automaticity.

Apply it to different contexts and use it to make links to other facts currently unknown.

Children have a strategy and understanding of the concept to start with, they can't ever learn and apply it. Not if they spend on times table games.

LANGUAGE IS THE KEY....

Addition:

$$8 + 3 = 11$$

Addend Addend Sum

Multiplication:

$$6 \times 3 = 18$$

Factor (or Multiplier) Factor (or Multiplicand) Product

Subtraction

$$8 - 3 = 5$$

Minuend Subtrahend Difference

Division

$$22 \div 5 = 4 \text{ R } 2$$

Dividend Divisor Quotient Remainder

dition:

$$8 + 3 = 11$$

Addend Addend Sum

$$8 - 3 = 5$$

Minuend Subtrahend Difference

HOW TO GENERALISE? LANGUAGE IS KEY

o addends are commutative.

e order matters for subtraction.

have a positive difference the minuend must be greater than the subtrahe



end $\rightarrow 22 \div 5 = 4 \text{ R } 2 \leftarrow$ Remainder

Divisor \uparrow Quotient

Multiplication:

$6 \times 3 = 18$

Factor (or Multiplier) \uparrow Factor (or Multiplicand) \uparrow Product

HOW TO GENERALISE? LANGUAGE IS KEY

odd factors are equal to an odd product.

divisor is 5 and the remainder is 1, what do you notice about the dividend?

factor is 5, the product ends in a 0 or 5.

$_ \times 5 = _0$ or $_ \times 5 = _5$

How many ways?

The missing numbers are positive whole numbers.

$$60 \div \square = 4 \times \square$$

Fill in the missing numbers.

Level 1: I can find a way

Level 2: I can find different ways

Level 3: I know how many ways there are

KS1 EXAMPL



Pairs of Numbers



If you have ten counters numbered 1 to 10, how many can you put into pairs that add to 10?

Can you use them all?
Say how you got your answer.

Now put the counters into pairs to make 12.

- Can you use them all?
- Say how you got your answer.

Now put the counters into pairs to make 13.

- Can you use them all?
- Say how you got your answer.

Now put the counters into pairs to make 11.






































- Can you use them all?
- Say how you got your answer.



Shapes Times Shape

The coloured shapes stand for eleven of the numbers from 0 to 12. Each shape is a different number.

Can you work out what they are from the multiplications below?

 x  x  = 	 x  = 
 x  = 	 x  = 
 x  = 	 x  = 
 x  = 	 x  = 
 x  = 	 x  = 
 x  = 	 x  = 



NUMBER TALKS

$$19 \times 37 =$$

$$567 \div 7 =$$

$$16 \times 6 =$$

$$19 \times 37$$

A

$$2 \times 37 = 74$$

$$74 \times 10 = 740$$

$$740 - 37 = 703$$

B

$$10 \times 37 = 370$$

$$370 \times 2 = 740$$

$$740 - 37 = 703$$

$$567 \div 7$$

A

$$56 \div 7 = 8$$

$$560 \div 7 = 80$$

$$7 \div 7 = 1 \quad 80 + 1 = 81$$

$$16 \times 6$$

A

$$16 \times 2 = 32$$

$$32 \times 3 = 96$$

B

$$15 \times 6 = 15 \times 3 \times 2$$

$$15 \times 3 = 45$$

$$\text{Double } 45 = 90 + 6$$

C

$$16 \times 6 = 8 \times 12$$

$$= 96$$

MASTERING NUMBER RECEPTION AND KS1



This project aims to secure firm foundations in the development of good number sense for all children from Reception through to Year 1 and Year 2. The aim over time is that children will leave KS1 with fluency in calculation and confidence and flexibility with number. Attention will be given to key knowledge and understanding needed in Reception classes, and progression through KS1 to support success in the future.

<https://vimeo.com/720204080/51598c196f>

<https://www.ncetm.org.uk/maths-hubs-projects/mastering-number-at-reception-and-ks1/>



Key Messages

1. Fluency demands more of students than memorisation of a single procedure or collection of facts. It encompasses a mixture of efficiency, accuracy and flexibility.
2. Quick and efficient recall of facts and procedures is important in order for students to keep track of sub-problems, think strategically and solve problems.
3. Fluency also demands the flexibility to move between different contexts and representations of mathematics, to recognise relationships and make connections, and to make appropriate choices from a whole toolkit of methods, strategies and approaches.